

Modeling and Simulation of Transmural Cellular Electromechanical Properties in Heart Failure

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Abstract

In this paper, we present a simulation study of transmural cellular electromechanical properties in heart failure based on a integrated and refined heart cell model of Luo-Rudy II model and modified Hunter-McCulloch-ter Keurs mechanical model. The results show that prolonged action potential duration (APD) and APD rate-adaptation are more obviously transmurally heterogeneous in heart failure than those in control hearts. The results suggest that the differences of the electrical responses between failing cells and normal cells can cause slowing relaxation of the Ca²⁺ transient, and the difference of the Ca²⁺-TnC concentrations between fast and slow myocytes in failing hearts is smaller than in nonfailing hearts. It results in a decrease of force, which might diminish the role of mechanoelectric feedback, and then induce an increase of transmural APD gradient that might cause arrhythmia in heart failure. These results are in good accordance with experimental findings reported in the literatures and this electromechanical cardiac cell model might be very useful for further modeling and simulation of heart failure at both the tissue and the whole organ levels.

1. Introduction

Heart failure (HF) has emerged as one of the largest threats to the public health in the world. The relationship between alterations of repolarization and arrhythmia mechanisms in HF remains largely unknown [1]. And effects of heart failure on the mechanical function of the heart are also difficult to assess experimentally.

In the past decades, many electrical and mechanical heart models have been developed and used to investigate cardiac properties. However, the electromechanical mechanism of heart failure is not exactly clear so far. In this paper, we present a simulation study of transmural cellular electromechanical properties in heart failure based on an integrated and refined heart cell model.

2. Methods

2.1. Cellular electrophysiology modeling

In this study, the modified Luo-Rudy II model [2] is

used to simulate action potential duration (APD) of fast contracting hearts (such as small rodents), whereas modified ten Tusscher et al. model [3] is used to simulate APD of slower contracting myocardium (such as cat, rabbit, dog). Compared to the slow contracting myocardium (Tusscher et al. model), the action potential in the faster myocardium (Luo-Rudy II model) has a higher amplitude and shorter duration. Based on experimental studies of electrophysiological heterogeneities in failing heart both in fast and slow myocytes, we modify the previous ventricular cell models.

Recent experiments have indicated that peak I_{Na} and I_{kl} density significantly decrease by 57% and 25% in human heart failure respectively [4]. There is also a reduction in the current density of I_{to1} and the reduction is different in the variable myocyte layers [3,5]. According to the results of experiments by Li et al. [6], the decrease of I_{Ks} in all three layers becomes more homogeneous in HF than that in nonfailing (NF) without a significant change in I_{Kr} [6]. The most common change of I_{CaL} is a significant slowing of the whole-cell current decay [7], while a significant enhancement of the peak average current of I_{CaL} in HF has been reported [8]. Studies also show that the altered Ca²⁺ transients of the HF human myocytes are largely dependent on reduced sarcoplasmic reticulum (SR) Ca²⁺ uptake, storage, and release [9]. So, a reduction of the buffered calcium in the SR is incorporated into the HF model. Other currents such as I_{NaK} , I_{bCa} and I_{bNa} are changed in the same way to Priebe-Beuckelmann (PB) model [10].

2.2. Modeling of mechanical properties of ventricular cells

The mechanical cell model is constructed based on Hunter-McCulloch-ter Keurs (HMT) model [11], which used a curve fitting equation to describe the intracellular calcium concentration $[Ca^{2+}]_i$:

$$Ca_i(t) = Ca_0 + (Ca_{max} - Ca_0) \frac{t}{\tau_{Ca}} e^{-t/\tau_{Ca}} \quad (1)$$

$$\frac{dCa_{TnC}}{dt} = \rho_0 Ca_i (Ca_{TnCmax} - Ca_{TnC}) - \rho_1 \left(1 - \frac{T}{\gamma \times T_0}\right) Ca_{TnC} \quad (2)$$

In this research, we replace (1) with $[Ca^{2+}]_i$ produced

by simulation of highly developed models of cardiac cell membrane ion channels and transporters, in which the calcium induced-calcium release from SR is considered and provides the source of free myoplasmic calcium. HMT model is based on the experiment data of rat and ferret that belong to fast contracting myocytes. Mechanically fast muscle models are characterized by an increase in the rate constant for Ca^{2+} reuptake into the SR as well as a higher dissociation constant for the Ca^{2+} -TnC complex [12]. As a result, we modify ρ_i of (2) in order to simulate slow contracting myocytes.

3. Results

3.1. Remodeling of heterogeneous AP and APD rate dependence in HF ventricular cells

Based on the experimental studies of transmural electrophysiological heterogeneities in HF [6, 13], cardiac AP characteristics (at 0.5-2Hz) are simulated in different ventricular cell types in control and in HF: epicardial, M and endocardial cells by changing the parameters setting (Fig.1 A). Fig.1 illustrates that HF causes transmural electrical remodeling and changes the transmural heterogeneity in APs, results to a reduction of transmural AP gradients which is same to some groups' findings [6]. But it is contrary to some recent findings [14]. Only in M cell, EADs can be observed when the pulses increase to 2 Hz in HF. It seems that M cells are more susceptible to EADs in failing hearts, as in response to cardioactive agents under nondiseased conditions.

We simulate the rate-dependence of APD in epicardial, midmyocardial, and endocardial layers of control and HF over a CL range from 4000ms to 400ms. And we can find APDs of cells in all myocardial layers increased as CL was slowed. In control and HF, APD reached an apparent steady-state value at CL of 2000 ms.

Most important for APD adaptation is I_{CaL} at fast rates [15], supported by the fact that eliminating I_{CaL} from the model reduced adaptation (CL range of 8000 to 400 ms) from 60 to 20 ms (66% decrease). I_{to1} also plays a role: its elimination reduces adaptation by 25%, which is decreased in repolarization may facilitates APD shortening at a fast rate.

3.2. Selective enhancement of APD prolongation in HF

Recent study of Akar et al. [16] show APD prolongation in HF was markedly heterogeneous causing a significant rise (by 109%) in transmural AP gradient. They find M and endocardial cells underwent a more enhanced prolongation of their APD and significantly more enhanced sensitivity to rate compared with epicardial cells [14].

Based on the APD rate dependence analysis above, we

simulated the AP shapes of different ventricular cell types in HF and the rate-dependence of APD again, with changing I_{CaL} in epicardial cell (Fig.2). Results show the prolonged APD and APD rate-adaptation is markedly transmural heterogeneous (greater TDR), particularly in epicardial cells which is shorter and smaller than other cells, causing a significant rise in the transmural AP gradient similar to experiment data [16].

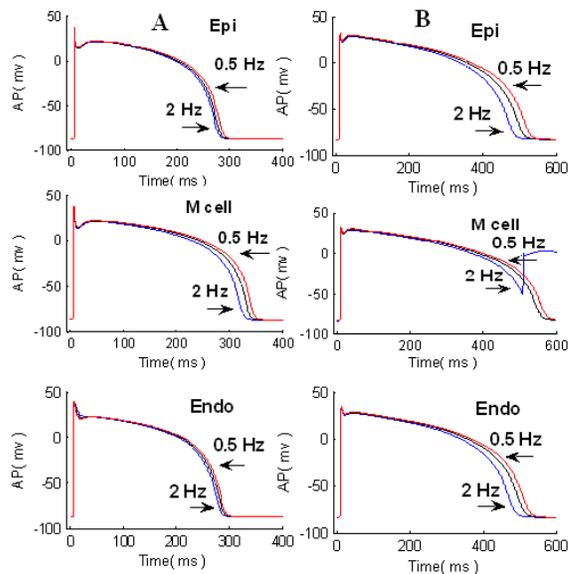


Fig.1. Simulated APs in cells from different regions of control and failing heart. A: AP in cells from the endocardium, midmyocardial layer (M cell), and epicardium showed heterogeneity in morphology and AP duration (APD) at 0.5, 1 and 2 Hz. B: APs simulated in cells from the Endo, M and epi layers of failing hearts.

3.3. Simulation of $[\text{Ca}^{2+}]_i$ of heterogeneous myocytes in heart failure

Based on experimental findings, compared to normal cells, the differences of the electrical responses in failing cells can cause reducing cardiac pump function due to the reducing of contractile force that may be the change of the intracellular Ca^{2+} transients ($[\text{Ca}^{2+}]_i$) and Ca^{2+} -TnC binding ($[\text{Ca}^{2+}$ -TnC]). We remodel the previous ventricular cell models with Ca handling by reducing SR Ca^{2+} uptake in the failing animal or human myocardium, which slows the decay of the Ca^{2+} transient and reduces SR Ca^{2+} stores [9]. This leads to reduce SR Ca^{2+} release, which induces additional Ca^{2+} influx during the plateau phase of the action potential, and further slow the decay of the Ca^{2+} transient. From Fig. 3A, C, model analyses demonstrate that the Ca^{2+} transient during the AP is markedly different in failing myocytes and NF ones, both for fast and slow contracting myocytes. So the concentrations of Ca^{2+} bound to the Ca-specific binding

site on TnC changes are obviously different in NF and failing hearts (Fig. 3B, D). But, interestingly, we find that the difference of the Ca^{2+} -TnC concentrations between fast and slow myocytes in failing hearts is much reduced than in NF hearts, which might cause a decrease of force difference in fast and slow myocytes in heart failure (Fig. 4). It corresponds well to experimental data [12].

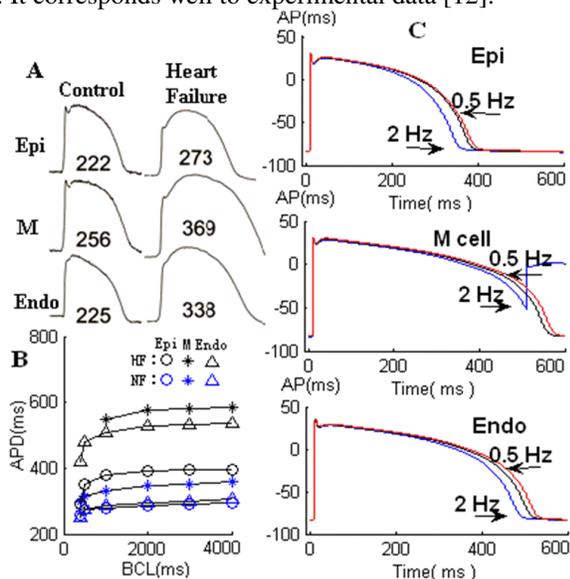


Fig.2. APD heterogeneities in failing myocardium. A: Representative APD recorded from the transmural of a control (left) and HF wedge (right). B: cycle length dependence of epicardial, M, and endo cardiac APD in control and HF. C: APs simulated in cells from the endo, M and epi layers of failing hearts with changed parameter setting of current I_{CaL} in Epi to explain enhancement transmural heterogeneities in HF.

3.4. Ca^{2+} transient induced force decrease in HF

On the basis of the analysis of the changes of Ca handling in NF and failing hearts, we simulate the isometric force in fast and slow myocytes (Fig. 4). We find that the amplitude of the isometric force both in fast and slow myocytes is decreased, as many investigators reported [17]. And we also find that the fast myocytes reach peak force earlier and relax faster than the slow ones [12] (Fig. 4) in NF hearts. Both fast and slow myocytes in heart failure, velocity of contraction is reduced and magnitude of contraction is attenuated [18]. Thus, in terms of the classical force-velocity concept, in heterogeneous myocardium, power is reduced in heart failure since both force and velocity are reduced [18].

One consequence of coupling the mechanics to electrophysiology is that the binding of Ca^{2+} to TnC alters the Ca^{2+} transient that affects Na^+ - Ca^{2+} exchange and hence APD. Mechanically induced changes in APD in

heterogeneous myocardium might explain the discrepancy of APD data of cells from different layers of the ventricular wall: isometric sub-epicardial (fast) cells tend to have shorter APD than isometric sub-endocardial (slow) ones, however, mechanoelectric feedback (MEF) may contribute to a reduction in transmural APD gradients in the intact human heart [5]. But In heart failure, a change of intracellular Ca^{2+} transients ($[Ca^{2+}]_i$) and Ca^{2+} -TnC binding ($[Ca^{2+}$ -TnC]) results in a decrease of force, which might diminish the role of MEF, then induce an increase of transmural APD gradients. It may explain that the electrophysiological heterogeneities in heart failure might contribute to arrhythmogeneity [16].

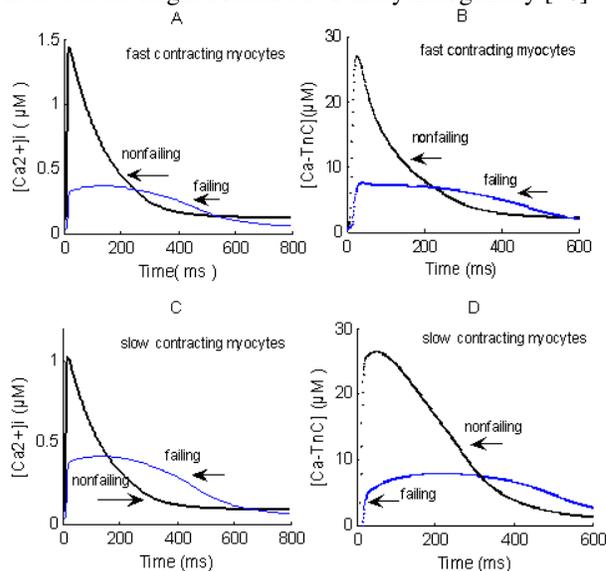


Fig.3. Simulation result of the intracellular $[Ca^{2+}]_i$ transient ($[Ca^{2+}]_i$) and the concentration of Ca^{2+} bound to TnC in a nonfailing and failing myocyte at a stimulation frequency of 0.5 Hz. (A), (B) fast myocytes. (C), (D) slow myocytes. (A), (C) the intracellular $[Ca^{2+}]_i$ transient ($[Ca^{2+}]_i$). (B), (D) the concentration of Ca^{2+} bound to TnC due to $[Ca^{2+}]_i$ in (A), (C) respectively.

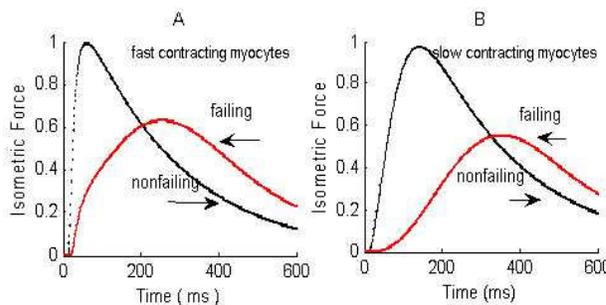


Fig.4. Contraction relaxation cycles in failing and nonfailing myocytes during isometric contractions. (A) fast myocytes. (B) slow myocytes.

4. Discussion and conclusions

In this paper, we present a simulation study of transmural cellular electromechanical properties in heart failure based on an integrated and refined heart cell model. In the electrical property investigation, we simulate the action potential shapes of different ventricular cell types, and determine the changes of transmural heterogeneity of cellular electrophysiology in nonfailing and failing hearts. The results show that prolonged action potential duration (APD) and APD rate-adaptation are more obviously transmural heterogeneous in heart failure than those in control heart, which may be due to enhanced transmural heterogeneities of I_{CaL} and I_{Ks} in myocytes. In the mechanical property investigation, we study cellular mechanical properties of both fast and slow contracting myocytes in heart failure. The results suggest that the differences of the electrical responses between failing cells and normal cells can cause slowing relaxation of the Ca^{2+} transient, and the difference of the Ca^{2+} -TnC concentrations between fast and slow myocytes in failing hearts is much reduced than in nonfailing hearts. It results in a decrease of force, which might diminish the role of MEF, then induce an increase of transmural APD gradients. It might cause arrhythmia in heart failure. These results are in good accordance with experimental findings reported in the literatures and this electromechanical cardiac cell model might be very useful for further modeling and simulation of heart failure at both the tissue and the whole organ levels.

However, the present model has several limitations. For example, in simulation of $[Ca^{2+}]_i$ transients, since the understanding of the exact mechanisms involved is incomplete, it is only an approximation of the complex nature of the intracellular Ca^{2+} homeostasis. Such problems should be further investigated in the future.

Acknowledgements

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