

# Modeling the Mechanism of $[Na^+]_i$ Elevation in Heart Failure by a Canine Ventricular Cell Model

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## Abstract

Numerous studies have found the phenomenon of  $[Na^+]_i$  elevation in cardiac myocytes in heart failure (HF), which may influence cardiac action potential (AP) and intracellular  $Ca^{2+}$  handling to induce cardiac arrhythmias. As one of the most important regulators in the cardiac myocytes,  $Ca^{2+}$ /Calmodulin-dependent protein kinase II (CaMKII), which could alter  $Na^+$  channel gating, was found to be over-expressed in HF. It may contribute to  $[Na^+]_i$  elevation in HF. For the purpose of this study, we developed a new canine epicardial cell model based on the framework of published Hund-Rudy dynamic (HRd) model. The effects of dynamic CaMKII regulation on fast  $Na^+$  current ( $I_{Na}$ ) and late  $Na^+$  current ( $I_{NaL}$ ) were incorporated into our model according to the recent experimental data. Simulation results suggested that the regulation role of CaMKII on  $I_{NaL}$  could elevate  $[Na^+]_i$ . The effect of COE on  $I_{Na}$  had a function of lowering  $[Na^+]_i$  in fact. However, it could not offset the trend of  $Na^+$  up-regulation by enhanced  $I_{NaL}$ . The magnitude of  $[Na^+]_i$  elevation was smaller than experimentally measured values. We speculate that other  $[Na^+]_i$  elevation mechanisms such as lowered  $Na^+/K^+$  pump ( $I_{NaK}$ ) or increased  $Na^+/H^+$  exchange may happen in HF.

## 1. Introduction

Heart failure (HF) is usually characteristic of prolonged APD facilitating cardiac arrhythmias and disturbed  $Ca^{2+}$  handling system causing contraction or relaxation dysfunction. Recently, more and more attention has been attracted to the phenomenon of  $[Na^+]_i$  elevation. Due to the interplay with  $Ca^{2+}$  by  $Na^+/Ca^{2+}$  exchange current ( $I_{NaCa}$ ), elevated  $[Na^+]_i$  may play a more important role in  $Ca^{2+}$  handling in HF. Some researchers even related it with a complementary mechanism for the lowered  $Ca^{2+}$  in HF [1]. However, the mechanism of  $[Na^+]_i$  elevation remains not clear. It is difficult for experiments to accurately find the mechanism because the cardiac myocyte is an interactive system and many

components of it affect each other. In this context, computer simulations provide an alternative way. Based on the framework of Hund-Rudy dynamic (HRd) model [2], we developed a new canine epicardial ventricular cell model to explore the mechanism of  $[Na^+]_i$  elevation in HF. Dynamic CaMKII kinetics was included. In HF, up-regulated CaMKII may be a possible reason of elevated  $[Na^+]_i$ .

## 2. Methods

In this work,  $Ca^{2+}$  handling system was reconstructed. Sarcoplasmic reticulum (SR)  $Ca^{2+}$  pump (SERCA) was modeled as a bidirectional pump [3]. SERCA and SR passive leakage current were dependent on both intracellular  $Ca^{2+}$  and  $Ca^{2+}$  in network SR ( $[Ca^{2+}]_{NSR}$ ). The SR release current was taken from Livshitz et al [4], which incorporated CaMKII dependent facilitation. Augmented  $I_{leak}$  by CaMKII over-expression (COE) was consistent with experimental observations [5]. Fast  $Na^+$  current ( $I_{Na}$ ), late  $Na^+$  current ( $I_{NaL}$ ), transient outward  $K^+$  current ( $I_{to}$ ), time-independent  $K^+$  current ( $I_{K1}$ ), rapid-activating delayed rectifier  $K^+$  current ( $I_{Kr}$ ), L-type  $Ca^{2+}$  current ( $I_{CaL}$ ) were reformulated using recent experimental data. The conductance of  $Na^+/K^+$  pump current ( $I_{NaK}$ ) was increased to stop  $[Na^+]_i$  accumulation. CaMKII kinetics was kept the same as in HRd model.

HF settings: Alterations in HF were grouped into two classes. The first class corresponded to acute COE regulated alterations of  $I_{CaL}$ , SERCA,  $I_{leak}$ ,  $I_{K1}$ ,  $I_{to}$ ,  $I_{Na}$  and  $I_{NaL}$ , which alterations could be reversed by CaMKII inhibitor. The second group corresponded to the protein expression remodeling of SERCA,  $I_{K1}$ , slow-activating delayed rectifier  $K^+$  current ( $I_{Ks}$ ) and  $I_{to}$ , which alterations could not be reversed by CaMKII inhibitor. In our simulation, SERCA was down-regulated by 50%, in the range of 49% to 52% estimated by Winslow et al [6].  $I_{K1}$  and  $I_{Ks}$  were down-regulated by 50% and 57%, respectively [7].  $I_{to,fast}$  was down-regulated by 30% and  $I_{to,slow}$  up-regulated by 41% [8].  $I_{NaCa}$  was not changed according to the experimental observations by Xiong et al [9].

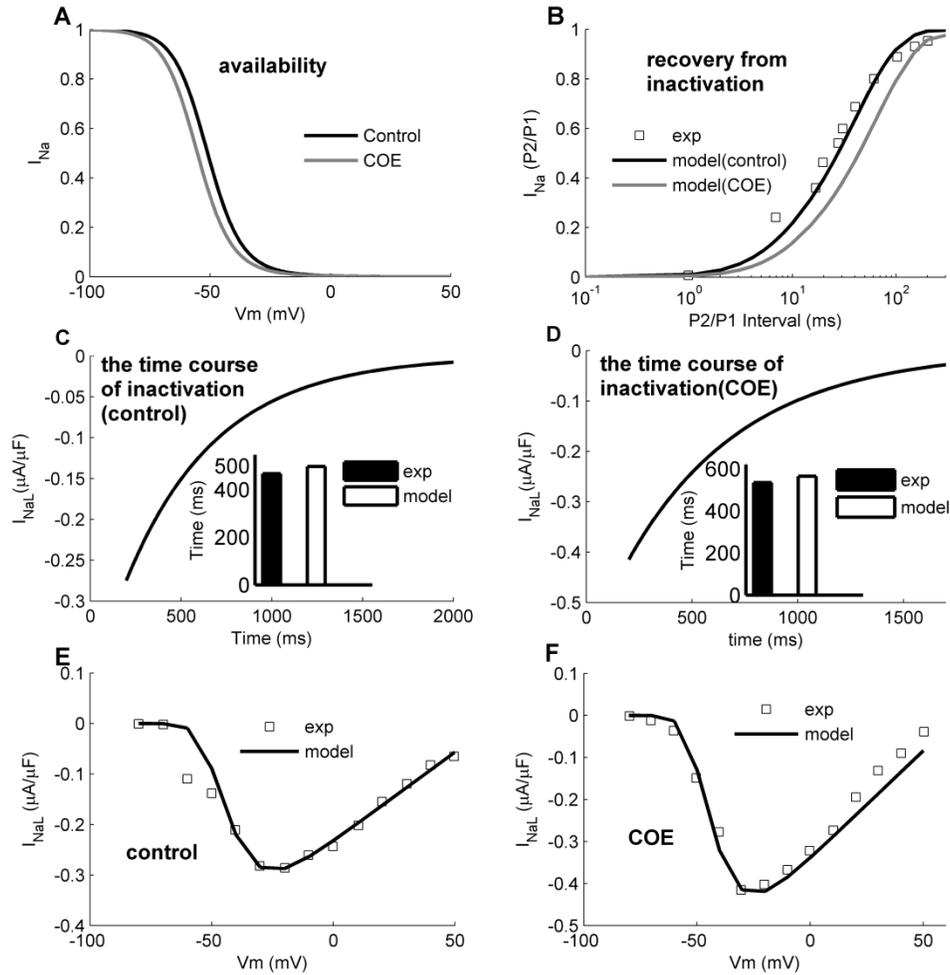


Figure 1. Gating properties of  $I_{Na}$  and  $I_{NaL}$ . (A)  $I_{Na}$  steady state inactivation in control and COE. (B)  $I_{Na}$  recovery from inactivation in control and COE. (C)  $I_{NaL}$  inactivation kinetics in control. (D)  $I_{NaL}$  inactivation kinetics in COE. (E)  $I_{NaL}$  I-V relationship in control. (F)  $I_{NaL}$  I-V relationship in COE.

### 3. Results

The gating properties of  $I_{Na}$  and  $I_{NaL}$  are shown in Figure 1. As shown in Figure 1B, the recovery kinetics of  $I_{Na}$  agrees well with experimentally measured values [10]. For  $I_{Na}$ , Steady state inactivation (SSI) was left shifted by 4.25 mV (Figure 1A) (-6 mV measured by Wagner et al (11)) and the recovery from inactivation was delayed by 58% (~50% measured by Wagner et al [11]) with COE. The conductance of  $I_{Na}$  was chosen to match the maximum upstroke velocity and AP amplitude from Lue et al [12]. Inactivation kinetics and I-V relationship of  $I_{NaL}$  were reformulated to match the recent experimentally measured values under both control and HF conditions [13] (Figure 1 C-F).

In control,  $[Na^+]$  at rest and 2 Hz are 6.65 mM and 10.3 mM respectively, which are in the range of experimentally measured values [14]. As shown in Figure

2, both under the condition of COE and HF, simulated  $I_{Na}$  at 1 Hz AP pacing is reduced which could cause lowered  $[Na^+]$ , whereas  $I_{NaL}$  show a trend to increase under the same circumstances. Augmented  $I_{NaL}$  would compensate the loss of  $[Na^+]$  by reduced  $I_{Na}$ . In response to the elevated  $[Na^+]$  and lowered intracellular  $[Ca^{2+}]$  In HF,  $I_{NaCa}$  spends a longer time in the reverse mode (i.e.  $Na^+$  efflux and  $Ca^{2+}$  influx state) (Figure 2C). At the same time,  $I_{NaCa}$  would tend to limit the  $[Na^+]$  accumulation to maintain its original state. However, the elevation of  $[Na^+]$  in our simulation (Figure 2D, 0.23 mM at 2 Hz, 0.3 mM at 1 Hz, 0.07 mM at 0.5 Hz) are smaller than experimentally observed values in HF (4 mM in canine [15]). To preclude the possibility that the discrepancy of our simulated  $[Na^+]$  elevation and experimental observations is due to the inaccuracy of the experimental

data which we used to model  $I_{NaL}$ , we tested another experimental data by Valdivia et al [16]. In that

experiment,  $I_{NaL}$  in HF has a nearly 3-fold increase compared with control. We implemented a 3-fold increase

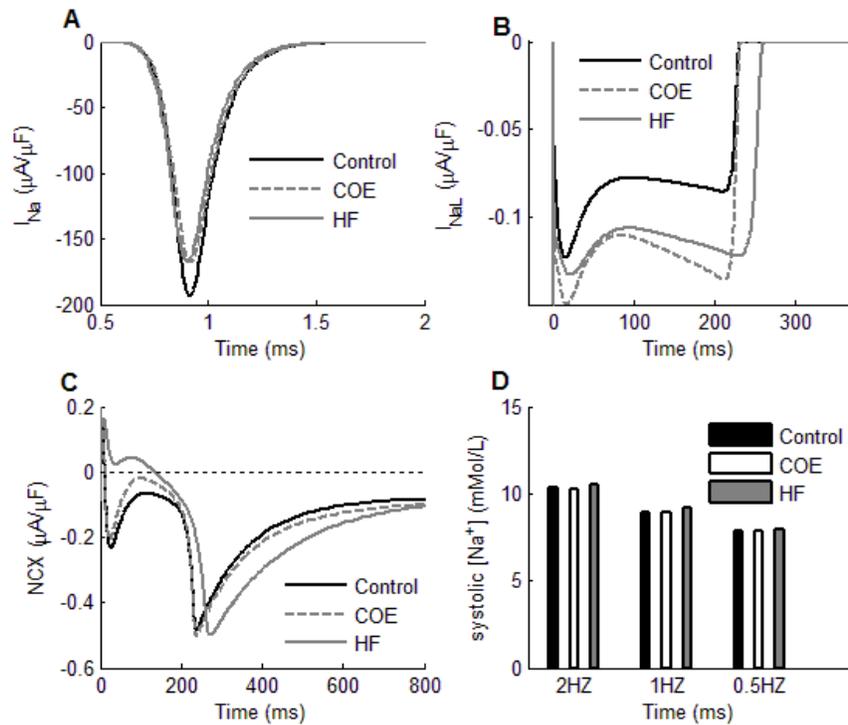


Figure 2.  $Na^+$  related currents and  $Na^+$  elevation. (A-C)  $I_{Na}$ ,  $I_{NaL}$ ,  $I_{NaCa}$  in control, COE and HF. (D)  $Na^+$  at different pacing rates in control, COE and HF.

in our HF simulation. However, in this simulation,  $[Na^+]$  had only another 0.2 mM elevation, still not close to the 4 mM elevation in HF. It suggests that there should be other mechanisms for  $[Na^+]$  elevation in HF [17].

#### 4. Discussion

$[Na^+]$  elevation mechanisms deduced from limited experimental data are controversial in some cases. According to Verdonck et al [15], dogs with hypertrophy showed a decrease in  $Na^+$  affinity of  $I_{NaK}$ , but Bossuyt et al found that  $I_{NaK}$  function was not altered in rabbits with HF [18]. According to experiments [11, 13], intracellular  $[Na^+]$  elevation was simulated by enhancing  $I_{NaL}$  alone in this work. However, 4 mM elevation was not achieved by

our model. There could be several explanations for this. Firstly,  $[Na^+]$  elevation may be species dependent and  $I_{NaK}$  may be down-regulated as reported [15]. In our model,  $[Na^+]$  is really sensitive to  $I_{NaK}$ . Even a small change in  $I_{NaK}$  could contribute to a big change on  $[Na^+]$ . Secondly, up-regulated  $Na^+/H^+$  exchange may also be a reason of  $[Na^+]$  elevation in HF [17]. In conclusion, we speculate that there should be other  $[Na^+]$  elevation mechanisms besides enhanced  $I_{NaL}$ .

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